

# Design of Cryogenic SiGe Low-Noise Amplifiers

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**Abstract**—This paper describes a method for designing cryogenic silicon-germanium (SiGe) transistor low-noise amplifiers and reports record microwave noise temperature, i.e., 2 K, measured at the module connector interface with a 50- $\Omega$  generator. A theory for the relevant noise sources in the transistor is derived from first principles to give the minimum possible noise temperature and optimum generator impedance in terms of dc measured current gain and transconductance. These measured dc quantities are then reported for an IBM SiGe BiCMOS-8HP transistor at temperatures from 295 to 15 K. The measured and modeled noise and gain for both a single- and two-transistor cascode amplifier in the 0.2–3-GHz range are then presented. The noise model is then combined with the transistor equivalent-circuit elements in a circuit simulator and the noise in the frequency range up to 20 GHz is compared with that of a typical InP HEMT.

**Index Terms**—Cascode, cryogenic, low-noise amplifier (LNA), noise parameters, silicon-germanium (SiGe).

## I. INTRODUCTION

REMARKABLE cryogenic performance in terms of cutoff frequency ( $>500$  GHz) and noise figure (NF) (0.3 dB at 14 GHz) have recently been reported for silicon-germanium (SiGe) HBTs [1], [2]. The device physics leading to these results is documented in [3] and excellent reviews of the technology with hundreds of references are in a recent special issue of the PROCEEDING OF THE IEEE [4]. The focus of this paper is low-noise amplifiers (LNAs) for very low noise ( $<0.1$ -dB NF) at frequencies under 20 GHz for applications where the noise in the generator (usually an antenna looking up) is well below 300 K. These applications are radio astronomy, space communications, low-temperature physics research, and IF amplifiers for cryogenic mixers operating above 100 GHz.

Design of LNAs requires a knowledge of a set of four noise parameters of the transistor ( $T_{\min}$ ,  $Z_{\text{opt}}$ , and  $R_n$  are one set) and also the small-signal equivalent-circuit model. For the amplifiers and transistors under consideration, the following three problems arise.

- 1) For very low noise transistors, it is difficult to measure the NF (and, hence, noise parameters) with an accuracy better than  $\pm 0.1$  dB due to uncertainty in the noise generator and losses in the noise parameter measuring equipment. Thus, the error is of the order of the NF we wish to measure.

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- 2) For SiGe HBTs, there are wide ranges of size and collector current to be considered and basic parameters such as current gain and transconductance vary widely with temperature and collector current. Thus, it is difficult to select an optimum device size, collector current, and embedding circuit.
- 3) The transistor small-signal equivalent circuit is usually known at room temperature, but not at cryogenic temperatures.

Our approach is to determine the transistor noise parameters from dc measurements, which are easily performed even at cryogenic temperatures. The operating temperatures, which are relevant and used for the measurements we report are: 1) 200 K for consideration of thermoelectric cooling; 2) 80 and 40 K for which small very long-life cryocoolers are available; and 3) 15 K, which is currently widely used with field-proven closed-cycle cryocoolers.<sup>1</sup>

An outline of this paper is as follows.

- 1) Derive from first principles a simple noise model, which only contains the noise mechanisms that dominate the cryogenic noise performance in the low microwave frequency range. This has been done many times in the past, but is repeated to reveal the underlying assumptions and to assure correctness for temperatures much different than 300 K.
- 2) The above low-frequency noise model requires only the knowledge of the current gain and transconductance as a function of collector current. Measurements of these quantities will be reported for SiGe transistors from the IBM SiGe BiCMOS-8HP 0.12- $\mu\text{m}$  process.
- 3) Using 1) and 2), the noise parameters are determined as a function of collector current  $I_C$  at the temperatures of interest.
- 4) The models will be validated by measurement of the noise temperature and gain of a transistor in a 50- $\Omega$  system,  $T'_{50}$  and  $S'_{21}$ , as a function of collector current and temperature.
- 5) The model will be extended by combining it with the small-signal equivalent circuit, especially the internal HBT capacitances  $C_{be}$  and  $C_{bc}$  to determine the noise parameters as a function of frequency.  $T_{\min}$  and  $Z_{\text{opt}}$  in the 0–20-GHz range will be compared with values for a typical InP HEMT.
- 6) A cascode amplifier operating from 0.5 to 3 GHz will be designed and measured as a function of frequency.

## II. SIMPLE LOW-FREQUENCY CRYOGENIC NOISE MODEL

A low-frequency noise model that shows the dominant sources of noise is shown in Fig. 1. Here,  $i_{BN}$  and  $i_{CN}$  are the shot noise generators due to the dc base and collector

<sup>1</sup>Cryodyne model 350 cryocooler, CTI Cryogenics Div., Brooks Automation, Mansfield, MA.

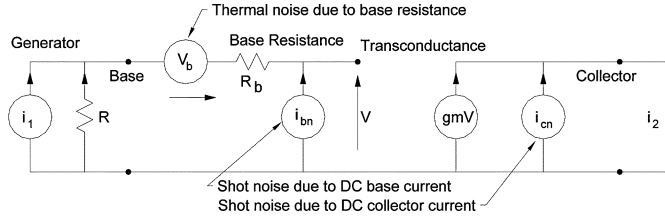


Fig. 1. Simple noise equivalent circuit of transistor.

bias currents. The correlation of these shot noise currents is controversial (see [5] and references therein), but our belief is that this correlation is negligible and that previous correlation measurements of input and output noise currents have been clouded by the correlation of terminal short circuit currents due to  $gm$  and  $R_b$ .

The noise temperature  $T_n$  of the transistor as a function of generator resistance  $R$  is equal to the temperature of  $R$ , which will produce the same thermal noise as all the noise sources in the transistor. We thus equate the output mean-square short-circuit current noise  $i_{2G}^2$  of the generator thermal noise to the same quantity due to the internal noise sources  $i_{2N}^2$

$$i_{2G}^2 = i_1^2 R^2 gm^2 \quad (1)$$

$$i_{2N}^2 = i_{CN}^2 + gm^2 v_b^2 + gm^2 R^2 i_{BN}^2. \quad (2)$$

$T_n$  can be determined in terms of useful parameters by equating (1) and (2) and using the shot noise relation  $i_n^2 = 2qI$ , where  $I$  is either the dc base current  $I_B$  or collector current  $I_C$ , the dc current gain  $\beta = I_C/I_B$ , and the thermal noise relations  $V_b^2 = 4kT_A R_b$  and  $i_1^2 = 4kT_n/R$ . The equation for  $T_n$  is more easily understood if the fundamental constants  $k$  and  $q$  are expressed in convenient units  $V_o = kT_o/q = 0.025$  V and  $T_o = 290$  K (independent of ambient temperature  $T_A$ )

$$\frac{T_n}{T_o} = \frac{T_A}{T_o} \frac{R_b}{R} + \frac{RI_C}{2V_o\beta} + \frac{RI_C}{2V_o} \frac{1}{R^2 gm^2}. \quad (3)$$

The terms are thus, from left to right, the contributions of base resistance thermal noise, base current shot noise, and the collector current shot noise. There is an optimum value of  $R$ , given below, which minimizes the noise, and this can be inserted in (3) to give  $T_{min}$ , the noise minimum with respect to  $R$

$$R_{OPT} = \left[ \frac{\beta}{gm^2} + \beta \frac{T_A}{T_o} \frac{2V_o R_b}{I_C} \right]^{1/2}. \quad (4)$$

In the case where the thermal noise of  $R_B$  is negligible, which is especially true for  $T_A \ll 290$  K,  $R_{OPT} = \sqrt{\beta/gm}$ . The minimum noise  $T_{MIN}$ , which can be achieved by the transistor in any circuit configuration<sup>2</sup> can be obtained by inserting (4) into (3). A good approximate value of  $T_{MIN}$ , valid for negligible contribution from  $R_B$ , is reached when the contribution from the base shot noise, proportional to  $R$  is equal to the contribution from collector shot noise proportional to  $1/R$ . In this case,

$$\frac{T_{MIN}}{T_o} \cong \frac{I_C/V_o}{gm\sqrt{\beta}} \quad (5)$$

<sup>2</sup>Lossless feedback can reduce the noise temperature of any amplifier to zero at the expense of power gain, but the noise temperature of cascaded stages, as expressed by noise measure, is invariant to lossless feedback [6].

which clearly shows the figure of merit  $I_C/(gm\sqrt{\beta})$  for minimum noise.

The selection of optimum  $I_C$  is much more difficult since  $\beta$  is a strong function of  $I_C$  at cryogenic temperatures and  $gm$  is not quite linear with  $I_C$ . Our procedure will be to measure  $\beta$  and  $gm$  as functions of  $I_C$  at the temperature of interest and then determine  $T_n$  and  $R_{opt}$  using (3) and (4).

The variation of  $T_n$  with scaling  $N$  of transistor size can also be determined from the measured dc data for one transistor by considering  $N$  transistors in parallel, but operated at a total collector current  $I_C$ . The measured single transistor  $\beta$  and  $gm$  at  $I_C/N$  are then used to determine the  $\beta$  and  $gm$  of the combination. The  $\beta$  for the combination is then the same (since both  $I_B$  and  $I_C$  are both multiplied by  $N$ ) and  $gm$  is given by  $N$  times the  $gm$  measured at  $I_C/N$ . Thus, if  $gm$  was a linear function of  $I_C$  then  $gm$  would be invariant to  $N$  for a given total  $I_C$ . For example if  $N = 10$ , evaluate  $\beta$  at the value measured at  $I_C/10$  and determine  $gm$  as 10 times the  $gm$  measured at  $I_C/10$ .

From consideration of the  $N$  parallel transistor case,  $R_{opt}$  is proportional to  $1/N$ . From the measured data to follow, it will be shown that large transistors are desirable to bring  $R_{opt}$  close to  $50 \Omega$  with  $I_C$  in a current density range for high cryogenic  $\beta$ . However, large transistors have high capacitance and a compromise dependant upon desired frequency and bandwidth is required.

### III. MEASUREMENTS OF $\beta$ AND $gm$ AS FUNCTIONS OF $I_C$ AND TEMPERATURE

A test strip of an IBM 8HP wafer processed in late 2006 was mounted with conductive epoxy in a coaxial test fixture, as shown in Fig. 2, and a  $3 \times 18 \times 0.12 \mu\text{m}$  HBT was bonded to coplanar waveguide (CPW) lines leading to subminiature (SMA) connectors and dc-bias tees. Two Keithley 2400 source meters were used in a computer-controlled setup to scan  $I_b$  and  $V_{ce}$ , while measuring  $V_{be}$  and  $I_C$ .

Raw data showing  $I_C$  versus  $V_{be}$  at six temperatures and  $I_C$  versus  $V_{ce}$  curves at 15 K are shown in the Appendix. The main attributes of the  $V_{be}$  curve are the increase of threshold voltage from approximately 0.8 V at 293 K to 1.05 V for temperatures below 40 K and an increase in slope ( $gm$ ) with cooling. The  $V_{ce}$  curves show little change in  $\beta$  with  $V_{ce}$  in the range of 0.2–1.2 V.

The most important experimental results of this paper are summarized in Figs. 3 and 4, which show  $\beta$  and  $gm$  as a function of  $I_C$  and temperature. The increase in  $\beta$  and  $gm$  by cooling from 293 to 40 K or less are remarkable.  $\beta$  increases by a factor of 20 (400–8000) and  $gm$  increases by 3.2 (10.1 dB). Applied in (5), these factors reduce  $T_{min}$  at a given  $I_C$  by a factor of 14.3

### IV. LOW-FREQUENCY CRYOGENIC NOISE AND GAIN MEASUREMENTS

It is important to note that the internal shot and thermal noise current sources are independent of frequency, although the noise currents reaching the device terminals are dependent upon frequency due to internal parasitic reactances. Thus, we can determine the noise sources at low frequencies where the parasitic effects are negligible and then determine the higher frequency

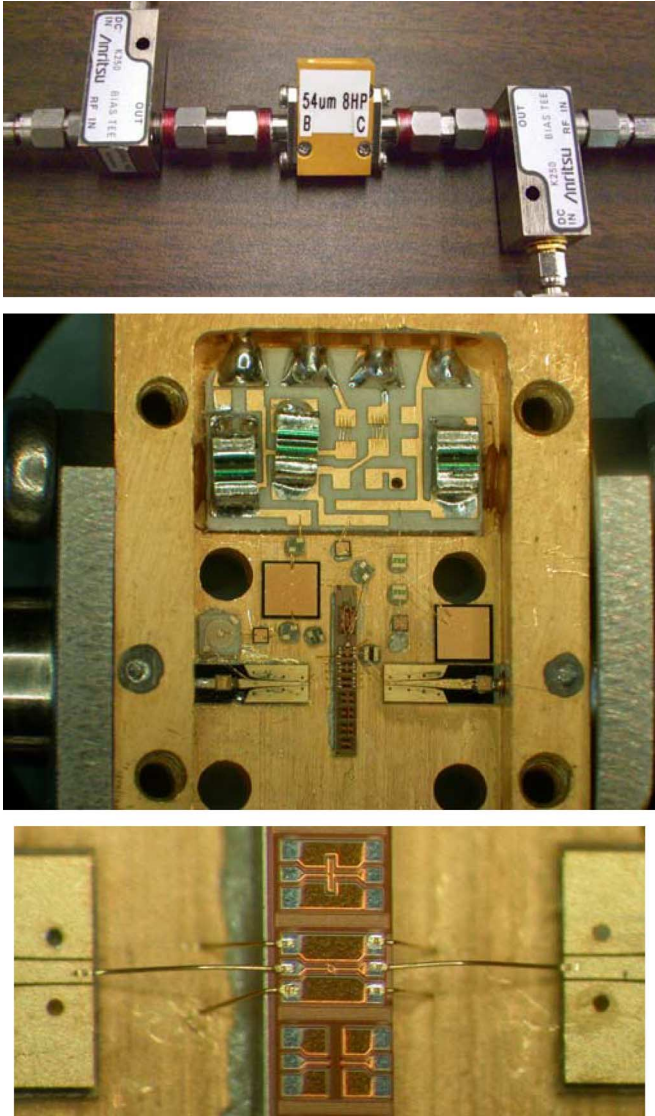


Fig. 2. (top) Coaxial test fixture with external dc-bias tee. (middle) Wafer segment bonded between 50- $\Omega$  lines. (bottom) Test transistor with bonds to base input, collector output, and emitter to ground.

effects in Section V by incorporating the device small-signal model determined from  $S$ -parameters.

The coaxial test fixture shown in Fig. 2 was modified to facilitate noise measurements by installing an internal input dc block (22-pF coupling capacitor and 50-K gate bias resistor) and bonding to an 180- $\mu\text{m}$  transistor ( $10 \times 18 \times 0.12 \mu\text{m}^2$ ), which has  $R_{\text{opt}}$  closer to 50  $\Omega$  than the 54- $\mu\text{m}$  device ( $3 \times 18 \times 0.12 \mu\text{m}^2$ ) used for dc characterization.

The test configuration shown in Fig. 5 was used for the cryogenic noise and gain measurements at frequencies in the 0.2–1.2-GHz range where both noise and gain have little variation with frequency. The lower frequency is determined by the 22-pF coupling capacitor and the upper frequency by capacitance within the transistor, which is to be included in Section V. A cryocooler was used to cool the amplifier and an input 20-dB attenuator to 15 K with higher temperatures available by applying power to a heating resistor affixed to the cold station. The input attenuator terminates the amplifier

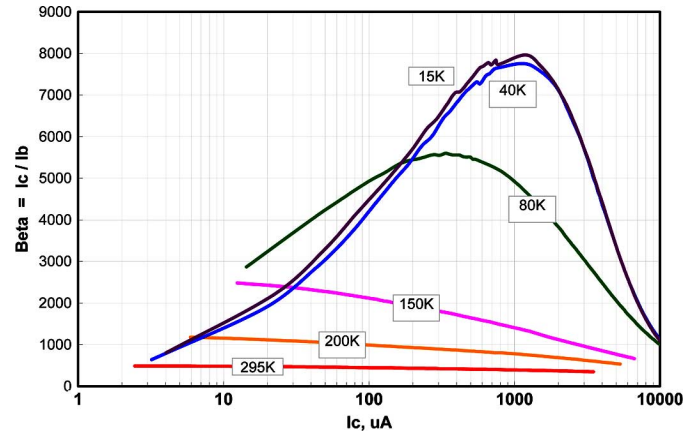


Fig. 3.  $\beta = I_C/I_b$  as a function of collector current at six temperatures for an IBM 8-HP 54- $\mu\text{m}$  SiGe transistor. The peak cryogenic  $\beta$  at  $I_C = 1000 \mu\text{A}$  thus occurs at a current density of  $0.15 \text{ mA}/\mu\text{m}^2$ , which is well below the current density for peak  $g_m$  or  $F_t$ .  $\beta$  is a function of current density and, thus, for example, a  $10 \times 18 \times 0.12\text{-}\mu\text{m}^2$  device would have peak  $\beta$  for temperatures  $< 40 \text{ K}$  at a collector current of 3.3 mA.

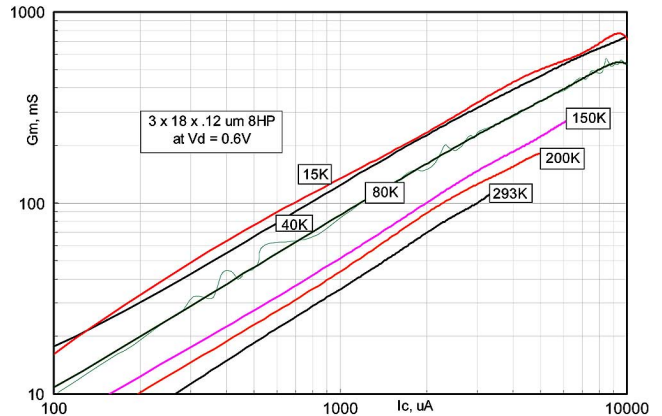


Fig. 4. Measured transconductance  $g_m$  as a function of collector current and temperature for an IBM 8 HP 54- $\mu\text{m}$  device. This data has been measured at dc as  $\partial I_C/\partial V_{be}$  and has been smoothed to remove measurement errors in the small increments. (Unsmoothed data is shown as dotted around the 80-K curve.) As an example of applying these curves, an 180- $\mu\text{m}$  device at 15 K would have a  $g_m$  of 1.02 S at 10 mA  $I_C$ , which is 3.3 times the value on the above curve at 3 mA.

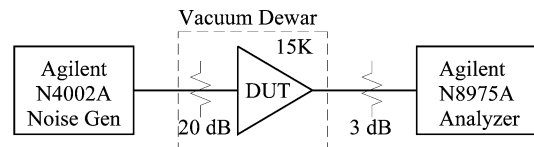


Fig. 5. Cryogenic noise test configuration. The cooled 20-dB attenuator at input of the device-under-test provides a calibrated low-temperature input termination and greatly increases the accuracy of low-noise measurements.

in a generator with 18-K noise (rather than 300 K without the attenuator) and greatly increases the accuracy of the cryogenic noise measurement. External to the vacuum chamber, an Agilent N4002A, 12–17-dB ENR “smart” noise source, and N8975A noise analyzer are utilized. This test set has been used for the noise measurement of over a 200 InP cryogenic LNA and comparison of the noise data with the National Institute of Standards and Technology (NIST) and other laboratories has indicated an accuracy of  $\pm 1 \text{ K}$  for frequencies up to 10 GHz.

TABLE I  
NOISE TEMPERATURE OF 180- $\mu\text{m}$  8-HP TRANSISTOR ALL AT  
 $V_{ce} = 0.6\text{V}$ ,  $I_C$  6–11 mA, AVERAGED 0.2–1.2 GHz

Quantity	Ambient Temperature, K				
	293	200	80	40	15
T50, measured, K	46.0	28.0	6.1	2.0	2.2
T50, at transistor, K	26.0	17.0	4.5	1.7	2.1
T50, modeled, K	23.5	15	4.7	2.5	1.8
Tmin, modeled, K	22.9	13	3.6	1.1	0.9
S21 measured, dB	23.9	27.9	32.0	32.5	32.8

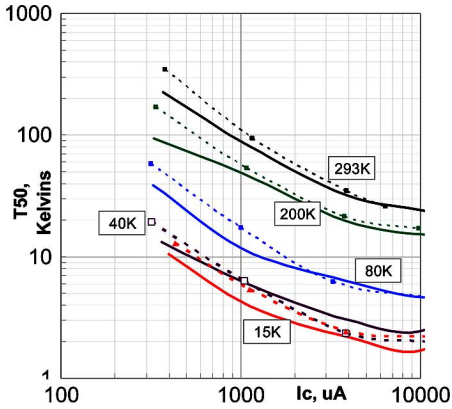


Fig. 6. Measured (dashed line) and modeled noise at 50- $\Omega$  generator impedance as a function of collector current and temperature for 180- $\mu\text{m}$  IBM 8-HP SiGe HBT. The noise temperature is averaged from 0.2 to 1.2 GHz with small deviations from the average in that frequency range.

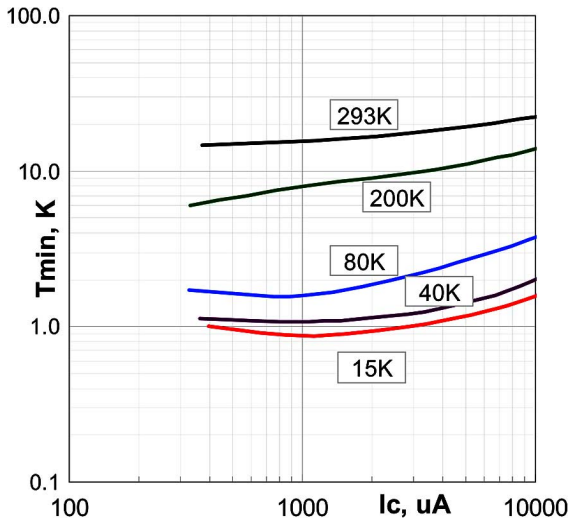


Fig. 7. Modeled minimum noise  $T_{min}$  achievable with optimum generator impedance  $R_{opt}$  for an 180- $\mu\text{m}$  IBM 8-HP HBT.

A summary of the noise results is given in Table I with more details in Figs. 6–9.

The noise temperature results are outstanding. To the best of our knowledge, the module noise is within  $\pm 1$  K of the lowest yet reported for a microwave amplifier. The results at 15 K are at a dc power of  $0.6\text{V} \times 7.1\text{ mA} = 4.2\text{ mW}$ . However, at  $0.15\text{ V} \times 3.3\text{ mA} = 0.5\text{ mW}$ , the noise only increased by 0.7 K and gain decreased by 3.2 dB. A tradeoff of power consumption

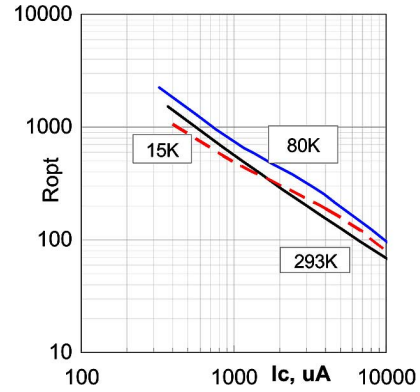


Fig. 8. Modeled low-frequency  $R_{opt}$  as a function of collector current at three temperatures for a 180- $\mu\text{m}$  device. There is little variation with temperature because the ratio of  $\sqrt{\beta}$  and  $gm$  in (4) do not vary by a large amount with temperature. The frequency variation of  $Z_{opt}$  at 15 K is shown in Fig. 11.

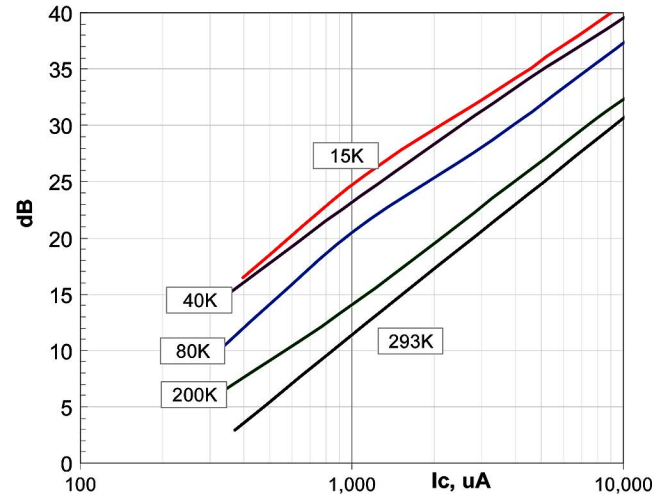


Fig. 9. Modeled low-frequency  $S_{21}$  versus  $I_C$  and temperature for the 180- $\mu\text{m}$  HBT.

versus gain compression power is thus available and is important for large arrays of cryogenic detectors or mixers.

The top row in Table I is the measured noise at the module SMA input connector. The second row is the noise referred to the transistor input pads and corrects for the loss of the connector, input transmission line, coupling capacitor, bond wires, and lines from the bond pads to the transistor. At 293 K this loss is estimated to be 0.27 dB, and this value is scaled down with temperature proportional to the microwave surface resistance, which goes as the root of the dc resistivity of copper as a function of temperature. At 40 K and below, the loss correction is negligible.

## V. NOISE VERSUS FREQUENCY MODEL

As a basis for future amplifier designs, a size-scalable small-signal noise model of an 8-HP HBT was analyzed in a circuit simulator [7]. The equivalent-circuit elements were determined from 300-K IBM model data with the addition of  $\beta$  and  $gm$  as a function of  $I_C$  and temperature from the measurements summarized in Figs. 3 and 4. Thus, the assumption is that the only equivalent-circuit elements that vary with temperature are  $\beta$  and  $gm$ . (Previous cryogenic  $S$ -parameter measurements [2]



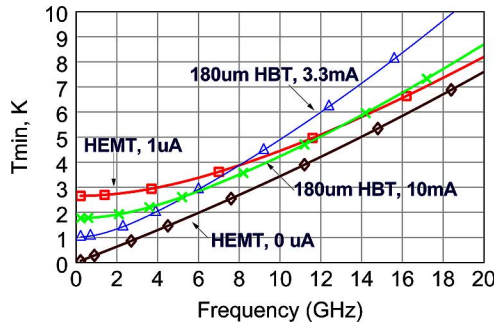


Fig. 10. Modeled minimum noise temperature as a function of frequency at 15 K for two HBTs and two InP HEMTs shown in Table II. The noise of the 54- $\mu\text{m}$  HBT at  $I_c = 3$  mA shown in column 1 of Table II is identical to that of the 180- $\mu\text{m}$  HBT at  $I_c = 10$  mA. The voltage and current per transistor are similar for InP and SiGe (around 0.8 V and 10 mA = 8 mW) and can be optimized if necessary for lower power at little increase in noise.

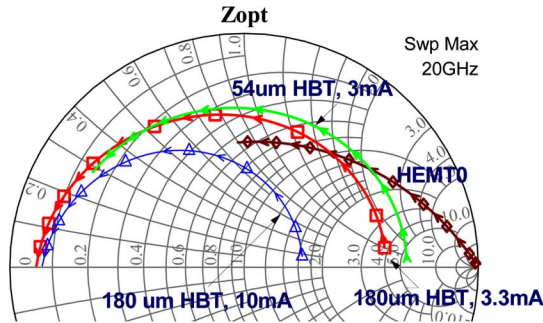


Fig. 11. Modeled optimum noise impedance  $Z_{opt}$ , 0.2–20 GHz, at 15 K for the cases shown in Table II. Note that if this impedance was expressed as an admittance, i.e.,  $Y_{opt}$ , then  $G_{opt}$  is more constant with frequency than  $R_{opt}$ .

TABLE II  
COMPARISON OF SiGe HBT AND HEMT AT 15 K

Case	1	3	4	HEMT0	HEMT1
Width, $\mu\text{m}$	54	180	180	200	200
$I_c$ , mA	3	10	3.3	6	6
Beta	5600	5600	7800	-	-
$g_m$ , mS	300	1000	470	220	220
$T_{min}$ , 1 GHz	1.8	1.8	1.1	0.4	2.7
$T_{min}$ , 8 GHz	3.5	3.5	3.9	2.7	3.9

have shown that the base resistance  $R_b$  is lowered by a factor of 2 with cooling and this would improve the noise at higher frequencies.)

The circuit simulator was used to compute  $T_{min}$ , the minimum noise temperature with respect to generator impedance, as well as the optimum value of this impedance  $Z_{opt}$ ; these results are shown in Figs. 10 and 11. The values, at 15 K, for three different cases of HBT size and  $I_c$ , are also tabulated in Table II.

For comparison with these results, 0.1- $\mu\text{m}$  InP HEMT transistors previously measured at 15 K [8], [9] have been included. The HEMT noise at low microwave frequencies depends upon the gate leakage current ranging from  $<0.1 \mu\text{A}$  (denoted as 0  $\mu\text{A}$  in Fig. 10) for selected transistors to 1  $\mu\text{A}$  for a mediocre transistor. The results show comparable noise temperatures. Improved devices of both types are expected with shorter gate (0.035  $\mu\text{m}$ ) HEMT devices now available and expectations of

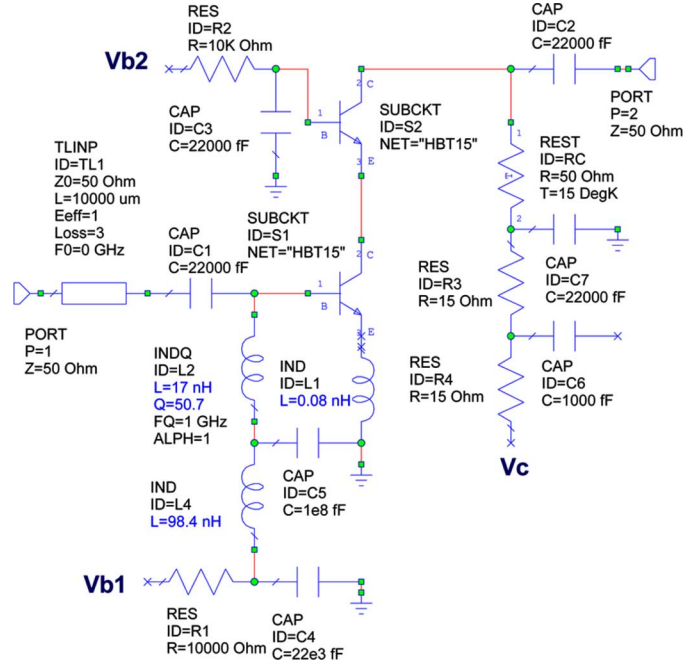


Fig. 12. Schematic of cascode 0.5–3-GHz amplifier modeled with circuit simulation software [7] and implemented as shown in Fig. 13 with bond-wire connections of small MIC components.

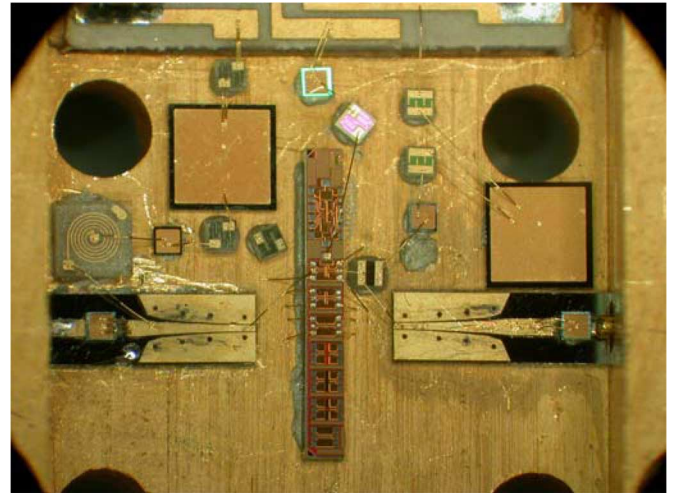


Fig. 13. Cascode amplifier implemented in a SMA connector module with internal dc blocks. The cascode of two transistors is within one 500- $\mu\text{m}$  square of the larger wafer strip containing other test circuits. An input spiral inductor,  $L_2$  on the schematic, is shown on the left and the collector load resistor  $R_C$  is to the right of the chip.

further improvement of SiGe HBTs. Note that the  $Z_{opt}$  reflection coefficient angle change with frequency for the HEMT device is approximately 1/2 that of the HBTs, and this will result in greater noise bandwidth. On the other hand, the HBTs have higher yield and offer the opportunity for large-scale integration.

## VI. CASCODE AMPLIFIER EXAMPLE

In order to further validate the design methods and demonstrate a simple extreme LNA. A single-stage cascode microwave integrated circuit (MIC) amplifier was assembled, as shown in Figs. 12 and 13, with measured and modeled results shown in

TABLE III  
MEASURED AMPLIFIER RESULTS AT 300 AND 15 K

Physical Temperature, K	300	15
Noise temperature, K, at 1 GHz	60	2.1
Gain, dB, at 1 GHz	22	28
Input return loss, dB, 0.5 to 5 GHz	> 2	NM
Output return loss, dB, 0.6 to 3 GHz	>12	>12

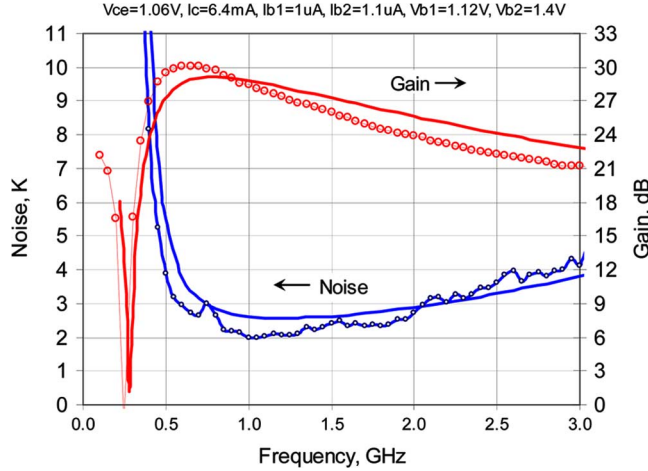


Fig. 14. Measured and modeled noise and gain of a single-stage cascode SiGe IBM 8-HP 180- $\mu\text{m}$  transistor at 15 K. We believe the large dip in gain at 0.25 GHz is due a resonance between two capacitors on the gate bias line and can be easily remedied.

Table III and Fig. 14. The noise is measured at an input SMA connector with no corrections for fixture loss. The shape of  $S_{21}$  and  $S_{22}$  did not change appreciably from 300 to 15 K, indicating that the reactive elements in the device equivalent circuit do not change by large amounts and confirming that the cryogenic dc measurements of  $\beta$  and  $gm$  in addition to the 300-K model are sufficient for cryogenic design.

This example amplifier was constructed with long bond-wire connections between existing undiced discrete transistor chips and is by no means optimum with respect to input return loss or gain flatness. The input return loss is poor due to the lack of feedback to improve input match. At frequencies above 6 GHz, the  $S$ -parameters vary widely and the output return loss is  $<0$  dB at 8 GHz; this is believed to be due to long bond-wire coupling and lack of proper layout. The 3-dB pad on the output, as shown in Fig. 5, assures stability and no oscillations were observed with a 26-GHz spectrum analyzer. A two-stage monolithic microwave integrated circuit (MMIC) amplifier removing these deficiencies has been designed and will be reported in a future publication.

## VII. CONCLUSION

We have demonstrated that SiGe bipolar transistors have excellent potential to become the device of choice for very low-noise cryogenic amplifiers required in radio astronomy, space communications, and other microwave applications where the generator noise is much less than 300 K. The measured noise temperature in the 0.7–3-GHz range and the modeled noise temperature to 20 GHz are comparable to that measured with the best 0.1- $\mu\text{m}$  InP HEMT transistors, yet SiGe has advantages of on-chip integration with CMOS, very high yield, a rich stable of accurate passive components, and a more rapid development

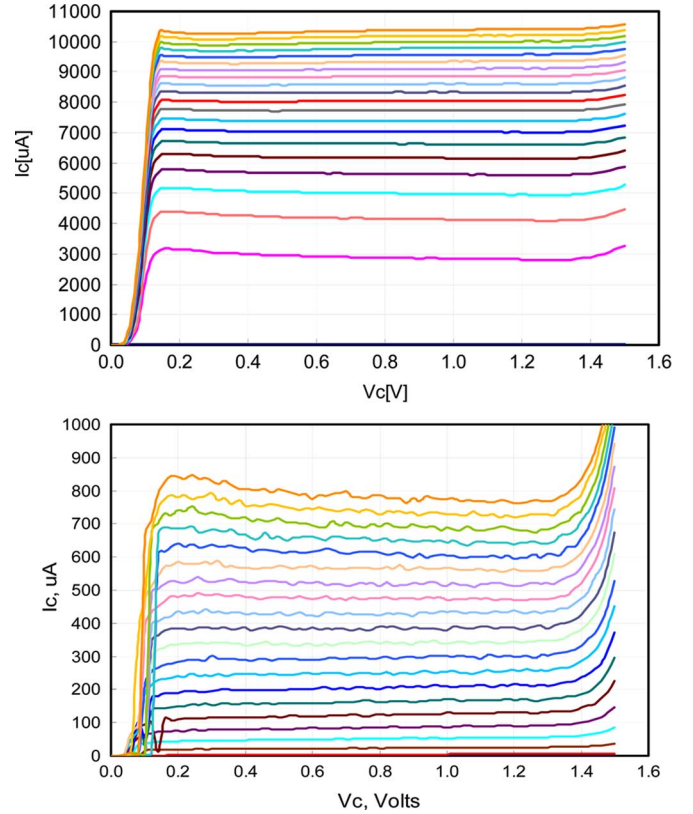


Fig. 15.  $I_C$  versus  $V_c$  at 15 K. (top) For 0.5- $\mu\text{A}$  steps of  $I_b$ . (bottom) For 5-nA steps.

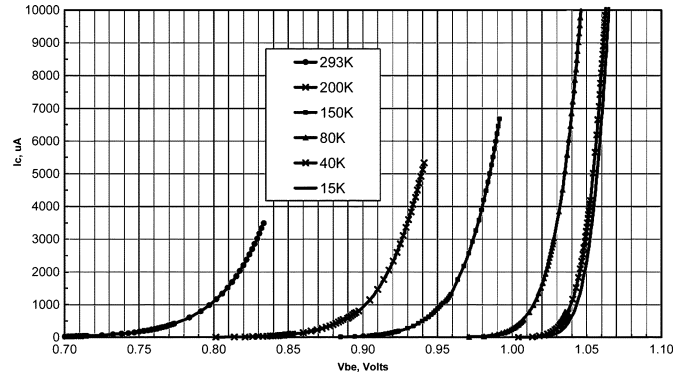


Fig. 16.  $I_C$  as a function of  $V_{be}$  at six temperatures. The slope gives the transconductance  $gm$ .

pace. This paper has demonstrated the design procedure of using dc measurements to determine a noise model as a function of temperature and collector current. This dc data in conjunction with a transistor small-signal model can then be used to determine the optimum device size, collector current, and generator impedance.

## APPENDIX

Additional cryogenic dc data for 54- $\mu\text{m}$  HBT is shown in Figs. 15 and 16.

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## REFERENCES

- [1] R. Krthivasan, Y. Lu, J. D. Cressler, J.-S. Rieh, M. H. Khater, D. Ahlgren, and G. Freeman, "Half-terahertz operation of SiGe HBTs," *IEEE Electron Device Lett.*, vol. 27, no. 7, pp. 567–569, Jul. 2006.
- [2] B. Banerjee, S. Venkataraman, Y. Lu, Q. Liang, C.-H. Lee, S. Nuttinck, D. Heo, Y.-J. E. Chen, J. D. Cressler, J. Laskar, G. Freeman, and D. C. Ahlgren, "Cryogenic operation of third-generation, 200-GHz peak  $f_T$  silicon-germanium heterojunction bipolar transistors," *IEEE Trans. Electron Devices*, vol. 52, no. 4, pp. 585–593, Apr. 2005.
- [3] J. D. Cressler and G. Niu, *Silicon-Germanium Heterojunction Bipolar Transistors*. Norwood, MA: Artech House, 2003.
- [4] R. Singe, D. Harame, and B. Myerson, Eds., *Proc. IEEE (Special Issue)*, vol. 93, no. 9, Sep. 2005.
- [5] M. A. Selim, "Accurate high-frequency noise modeling in SiGe HBTs," *RF Design*, pp. 24–32, Mar. 2006.
- [6] H. A. Haus and R. B. Adler, "Optimum noise performance of linear amplifiers," *Proc. IRE*, vol. 46, no. 8, pp. 1517–1533, Aug. 1958.
- [7] Microwave Office, ver. 6.53, Appl. Wave Res., El Segundo, CA.
- [8] R. Grundbacher, R. Lai, M. Barsky, R. Tsai, T. Gaier, S. Weinreb, D. Dawson, J. J. Bautista, J. F. Davis, N. Erickson, T. Block, and A. Oki, "0.1- $\mu\text{m}$  InP HEMT devices and MMICs for cryogenic low noise amplifiers from  $X$ -band to  $W$ -band," in *14th Indium Phosphide and Related Mater. Conf.*, May 2002, pp. 455–458.
- [9] J. D. Pandian, L. Baker, G. Cortes, P. F. Goldsmith, A. A. Deshpande, R. Ganesan, J. Hagen, L. Locke, N. Wadefalk, and S. Weinreb, "Low-noise 6–8 GHz receiver," *IEEE Micro*, vol. 7, no. 6, pp. 74–84, Dec. 2006.



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